



# Tuning rules for feedforward compensators combined with PID control



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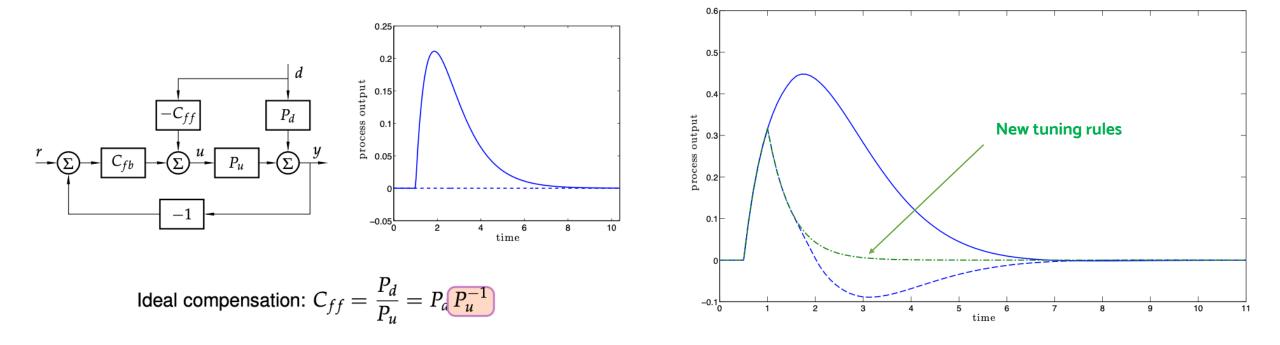






## What will we see in this presentation?





J. L. Guzmán, T. Hägglund. Tuning rules for feedforward control from measurable disturbances combined with PID control: A review. International Journal of Control, 2021.

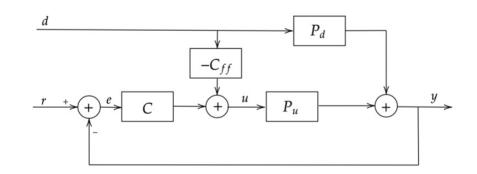


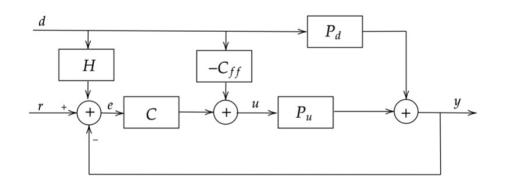
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## What will we see in this presentation?







CS	Rule	м	k <sub>ff</sub>	T <sub>p</sub>	Tz
С	1	OS	$(K_d/K_u)e^{(L_d-L_u)/T_d}$	$T_d$	$T_u$
с	2	OS	$\frac{\mathbf{k_{ff}}}{(K_d/K_u)e^{(L_d-L_u)/T_d}}$ $\frac{K_d(T_u+\lambda)}{K_u(T_d+\lambda)}\epsilon  T_u \neq T_d$ $\frac{K_d}{K_u}e^{(L_d-L_u)/T_d}  T_u = T_d$ $\epsilon = e^{(L_u/(T_u+\lambda)-L_d/(T_d+\lambda))}$	_	-
С	3	OS	$K_d/K_u - (K/\tau_i)IE$	$T_d$	$T_u$
С	4	OS	$K_d/K_u - (K/\tau_i)IE$	$\frac{T_d - (L_u - L_d)/4}{T_d}$	$T_u$
С	5	IAE	$(K_d (T_d + L_d))/(K_u (T_d + L_u))$	$T_d$	$T_u$
С	6	IAE	$\begin{aligned} \frac{K_d(T_u+\lambda)}{K_u(T_d+\lambda)}\theta & T_u \neq T_d \\ \frac{K_d(T_d+L_d)}{K_u(T_d+L_u)} & T_u = T_d \\ \theta = e^{-(L_u-L_d+(T_u-T_d)\log(2))/(T_d+\lambda)} \end{aligned}$	_	-
C	7	IAE	$K_d/K_u - (K/ au_i)IE$	$\frac{T_d - (L_u - L_d)/1.7}{T_d}$	$T_u$
C	8	ISE	$(K_d/K_u)e^{-(L_u-L_d)/(\lambda+T_d)}$		$T_u$
С	9	ISE	$K_d/K_u - (K/ au_i)IE$	$T_d - (L_u - L_d)/lpha \ lpha = rac{L}{2T_d \left(1 - e^{-L/(2T_d)} ight)}$	$T_u$
С	10	IAE ISE OS	$K_d/K_u - (K/ au_i)IE$	$     \begin{aligned}             T_d - (L_u - L_d) / \alpha \\             \frac{L}{2 T_d \left(1 - e^{-L/(2T_d)}\right)} & \text{ISE} \\             1.7 & \text{IAE} \\             4 & \text{OS}         \end{aligned}     $	$T_u$
в	11	ISE	$K_d/K_u$	$a = T_u/T_d$ $b = a(a+1)e^{L/T_d}$	$(T_p + T_u)\eta$ $\eta = \left(1 - \frac{2T_u}{b(T_d + T_p)}\right)$
B IE -	12	IAE ISE	$K_d/K_u$ + $T_u - T_d + T_p - T_z$ )	$\begin{split} \widehat{T_d} &- (\widehat{L_u} - L_d)/\alpha \\ \alpha &= \begin{cases} \frac{L}{2T_d \left(1 - e^{-L/(2T_d)}\right)} & \text{ISE} \\ 1.7 & \text{IAE} \end{cases} \end{split}$	$T_u$

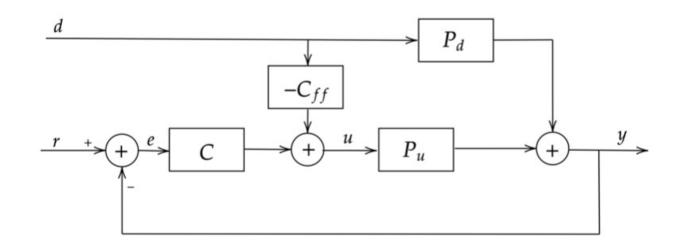


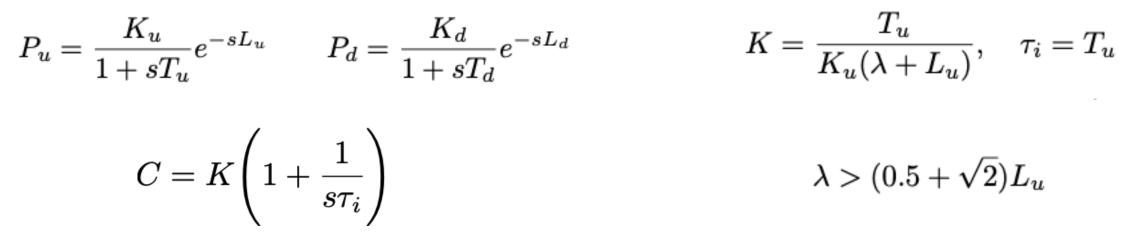












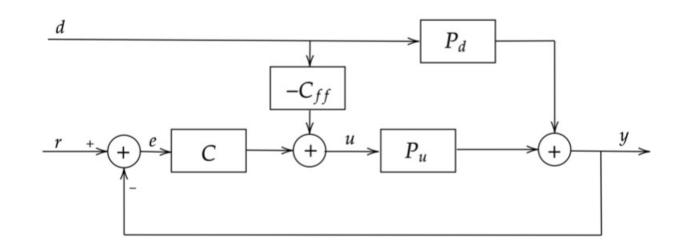


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$$G_{y/d} = \frac{P_d - P_u C_{ff}}{1 + CP_u} \qquad C_{ff} = k_{ff} \frac{sT_z + 1}{sT_p + 1} e^{-sL_{ff}}$$
$$C_{ff} = \frac{P_d}{P_u} \qquad C_{ff} = \frac{K_d}{K_u} \frac{sT_u + 1}{sT_d + 1} e^{-s(L_d - L_u)}$$

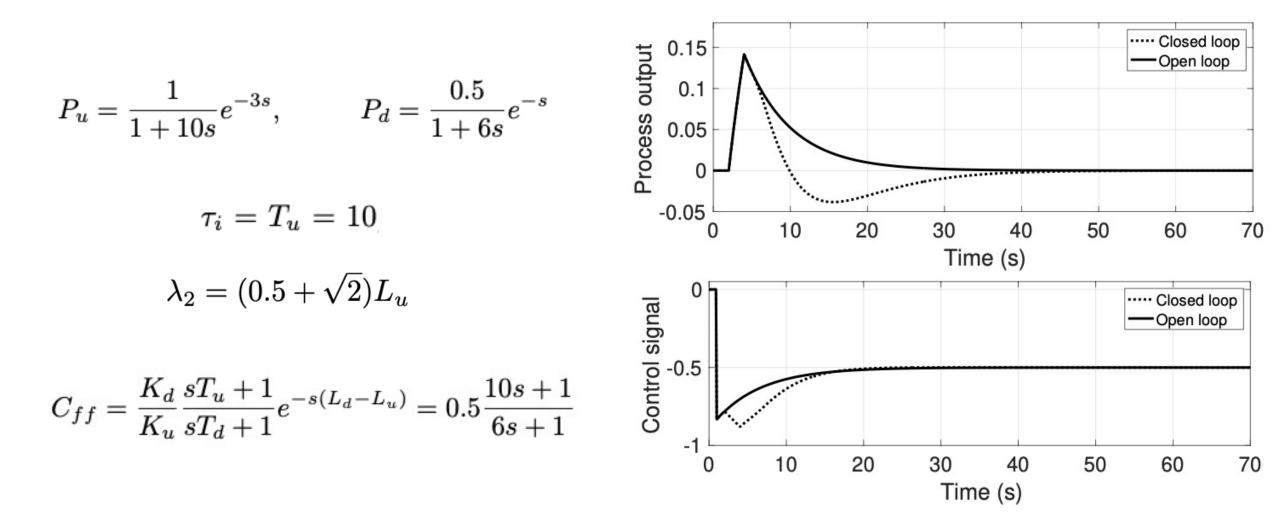


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Preliminaries



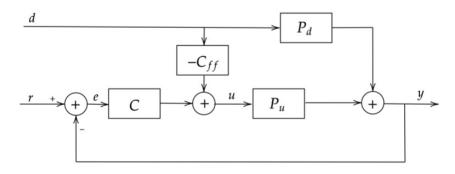


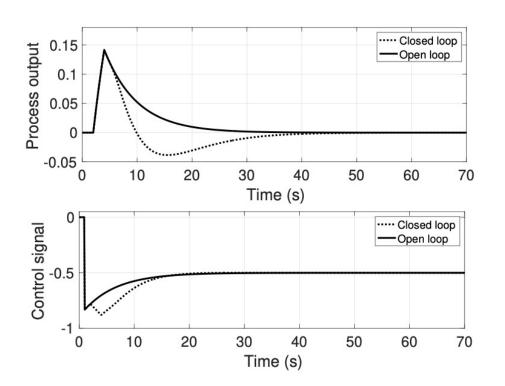


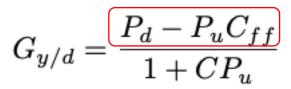
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**Residual term!** 

#### Feedback and feedforward interaction!

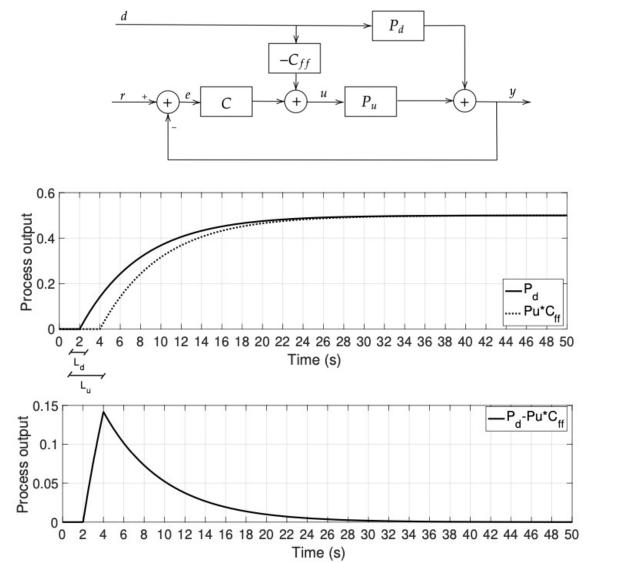


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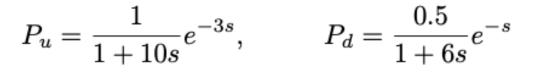




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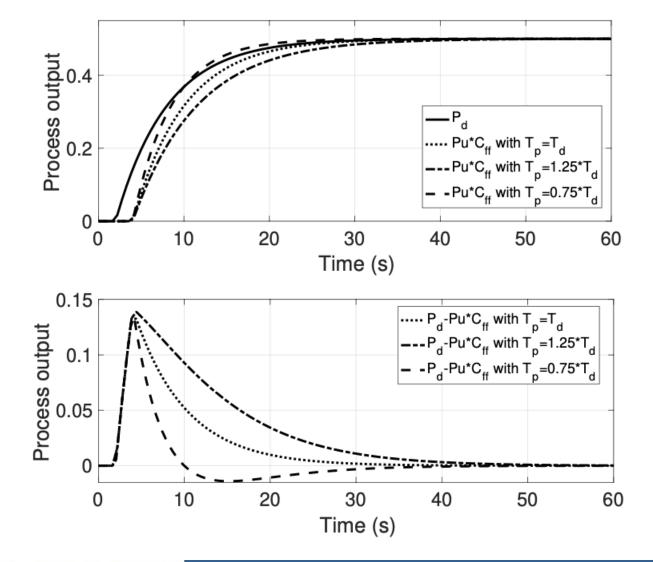
$$G_{y/d} = \frac{P_d - P_u C_{ff}}{1 + CP_u}$$



$$C_{ff} = \frac{K_d}{K_u} \frac{sT_u + 1}{sT_d + 1} e^{-s(L_d - L_u)} = 0.5 \frac{10s + 1}{6s + 1}$$







$$G_{ol} = P_d - P_u C_{ff}$$

## There is room for improvment!

VOKOHAMA

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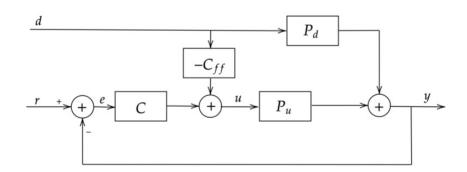


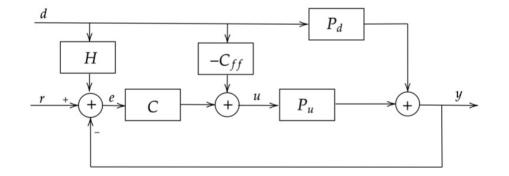


#### **Classical solutions for inversion problems in industry?**

Static feedforward

Non-interactive scheme





 $\mathbf{F}(a)$ 

$$C_{ff} = k_{ff} = \frac{K_d}{K_u}$$

$$G_{e/d} = \frac{E(s)}{D(s)} = \frac{H - P_d + P_u C_{ff}}{1 + CP_u}$$

$$H = P_d - P_u C_{ff}$$





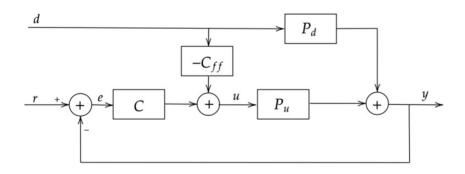




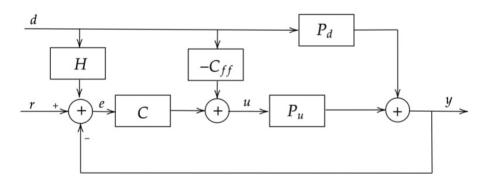




#### **Classical scheme**



Non-interactive scheme



Use the classic feedforward control scheme and tune the feedforward compensator properly. This means that the feedback controller C must be taken into account in the design.

Use the non-interacting feedforward control scheme and tune the feedforward compensator properly. The design can be made without taking feedback controller C into account.









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**Inversion problems** 

• Non-realizable delay inversion.

- Right-half plane zeros.
- Integrating poles.

**Tuning rule objective** 

- Minimize IAE.
- Minimize ISE.
- Reduce overshoot.

#### 15 different tuning rules for feedforward compensators!





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CS	Rule	Μ	$\mathbf{k_{ff}}$	T <sub>p</sub>	Tz
С	1	OS	$(K_d/K_u)e^{(L_d-L_u)/T_d}$	$T_d$	$T_u$
С	2	OS	$\frac{K_d(T_u + \lambda)}{K_u(T_d + \lambda)}\epsilon \qquad T_u \neq T_d$ $\frac{K_d}{K_u}e^{(L_d - L_u)/T_d} \qquad T_u = T_d$ $\epsilon = e^{(L_u/(T_u + \lambda) - L_d/(T_d + \lambda))}$	_	-
С	3	OS	$K_d/K_u - (K/ au_i)IE$	$T_d$	$T_u$
C	4	OS	$K_d/K_u - (K/ au_i)IE$	$\frac{T_d - (L_u - L_d)/4}{T_d}$	$T_u$
С	5	IAE	$(K_d (T_d + L_d))/(K_u (T_d + L_u))$	$T_d$	$T_u$
С	6	IAE	$ \begin{array}{c} \displaystyle \frac{K_d(T_u+\lambda)}{K_u(T_d+\lambda)}\theta & T_u \neq T_d \\ \displaystyle \frac{K_d(T_d+L_d)}{K_u(T_d+L_d)} & T_u = T_d \\ \displaystyle \frac{K_d(T_d+L_d)}{K_u(T_d+L_u)} & T_u = T_d \\ \displaystyle \theta = e^{-(L_u-L_d+(T_u-T_d)\log(2))/(T_d+\lambda)} \end{array} $	_	-
С	7	IAE	$K_d/K_u - (K/ au_i)IE$	$\frac{T_d - (L_u - L_d)/1.7}{T_d}$	$T_u$
С	8	ISE	$(K_d/K_u)e^{-(L_u-L_d)/(\lambda+T_d)}$	$T_d$	$T_u$
С	9	ISE	$K_d/K_u - (K/ au_i)IE$	$\frac{T_d - (L_u - L_d)/\alpha}{\alpha = \frac{L}{2T_d \left(1 - e^{-L/(2T_d)}\right)}}$	$T_u$
С	10	IAE ISE OS	$K_d/K_u - (K/ au_i)IE$	$\alpha = \begin{cases} T_d - (L_u - L_d)/\alpha \\ \frac{L}{2T_d(1 - e^{-L/(2T_d)})} & \text{ISE} \\ 1.7 & \text{IAE} \\ 4 & \text{OS} \end{cases}$	$T_u$
в	11	ISE	$K_d/K_u$	$a = T_u/T_d$ $b = a(a+1)e^{L/T_d}$	$(T_p + T_u)\eta$ $\eta = \left(1 - \frac{2T_u}{b(T_d + T_p)}\right)$
B	12	IAE ISE	$K_d/K_u$ + $T_u - T_d + T_p - T_z$ )	$\begin{aligned} T_d &- (L_u - L_d)/\alpha \\ \alpha &= \begin{cases} \frac{L}{2T_d \left(1 - e^{-L/(2T_d)}\right)} & \text{ISE} \\ 1.7 & \text{IAE} \end{cases} \end{aligned}$	$T_u$

Static  $C_{ff} = k_{ff}$ 

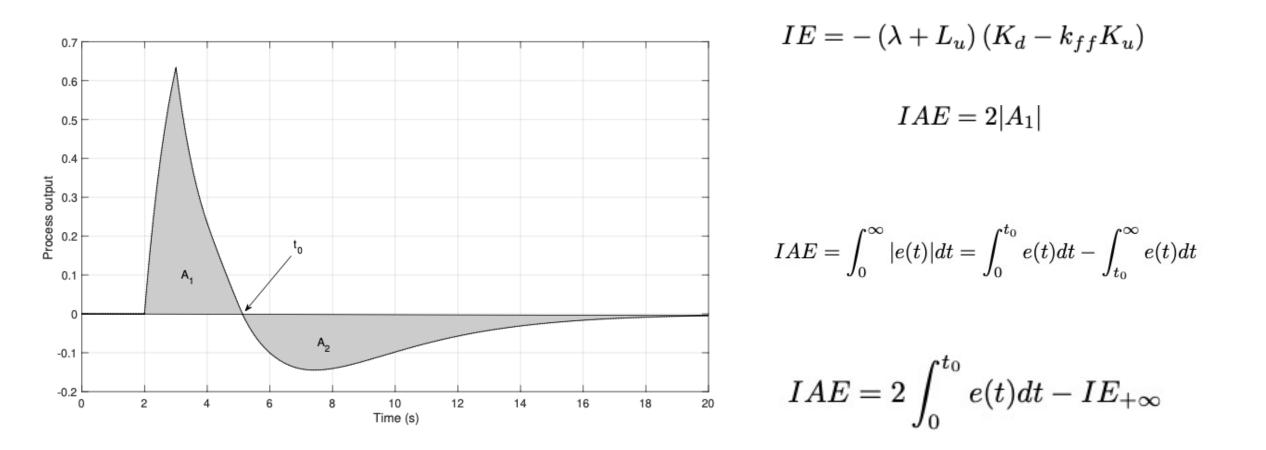
Lead - lag 
$$C_{ff} = k_{ff} \frac{1 + sT_z}{1 + sT_p}$$



















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$$P_{ff} = \frac{K_d e^{-sL_d}}{1+sT_d} - \frac{K_u e^{-sL_u}}{1+sT_u} C_{ff} \qquad \qquad E(s) = G_{e/d} \frac{1}{s} = -(\lambda + L_u) \left( \frac{sK_d e^{-sL_d}}{(sT_d + 1)(s\lambda + 1)} - \frac{sC_{ff} K_u e^{-sL_u}}{(sT_u + 1)(s\lambda + 1)} \right) \frac{1}{s}$$

$$G_{ol} = \frac{Y}{D} = \underbrace{P_d - P_u C_{ff}}_{P_{ff}} \qquad \qquad S = \frac{1}{1 + K \frac{1 + s\tau_i}{s\tau_i} K_u \frac{1 - sL_u}{sT_u + 1}} = \frac{(\lambda + L_u)s}{\lambda s + 1}$$

$$y_{ol}(t) = \begin{cases} 0 & : 0 \le t < L_d \\ K_d \left(1 - e^{(L_d - t)/T_d}\right) d & : L_d \le t < L_u \\ \mathcal{L}^{-1} \{P_{ff}D\} & : t \ge L_u \end{cases} \qquad \qquad y_{e/d}(t) = \begin{cases} 0 & : 0 \le t < L_d \\ -\frac{K_d (\lambda + L_u) \left(e^{(L_d - t)/T_d}/T_d - e^{(L_d - t)/\lambda}/\lambda\right)}{\lambda - T_d} d & : L_d \le t < L_u \\ \mathcal{L}^{-1} \{P_{ff}SD\} & : t \ge L_u \end{cases}$$

J. L. Guzmán, T. Hägglund. Tuning rules for feedforward control from measurable disturbances combined with PID control: A review. International Journal of Control, 2021.









#### **Classical scheme**

**Rule 7** Tuning rule for the classical control scheme to minimize IAE with a lead-lag compensator:

1. Set 
$$T_z = T_u$$
 and  $L_{ff} = \max(0, L_d - L_u)$ 

2. Calculate  $T_p$  as:

$$T_p = \begin{cases} T_d & L_u - L_d \leq 0 \\ T_d - \frac{L_u - L_d}{1.7} & 0 < L_u - L_d < 1.7 T_d \\ 0 & L_u - L_d > 1.7 T_d \end{cases}$$

3. Calculate the compensator gain  $k_{ff}$  as:

$$k_{ff} = \frac{K_d}{K_u} - \frac{K}{\tau_i} IE$$

$$IE = \begin{cases} K_d \ (T_u - T_d + T_p - T_z) & L_d \ge L_u \\ K_d \ (L_u - L_d + T_u - T_d + T_p - T_z) & L_d < L_u \end{cases}$$
4. End of design.

Non-interactive scheme

**Rule 12** Tuning rule for the non-interacting control scheme to minimize  
ISE, IAE, or to remove the overshoot with a lead-lag compensator.  
1. Set 
$$k_{ff} = K_d/K_u$$
,  $T_z = T_u$  and  $L_{ff} = \max(0, L_d - L_u)$ .  
2. Calculate  $L = L_u - L_d$ .  
3. Calculate  $\alpha$  depending on the desired behaviour:  
 $\alpha = \begin{cases} \frac{L}{2T_d(1-e^{-L/(2T_d)})} & aggressive (ISE minimization) \\ 1.7 & moderate (IAE minimization) \\ 4 & conservative (overshoot removal) \end{cases}$   
4. Set  $T_p$  according to:  
 $T_p = \begin{cases} T_d & L \leq 0 \\ T_d - \frac{L}{\alpha} & 0 < L < \alpha T_d \\ 0 & L \geq \alpha T_d \end{cases}$   
If  $T_p = 0$ , select a value close to zero to obtain a realizable compen-  
sator.  
5. Set  $H(s)$  with Equation (4.66) for the non-interacting scheme.

J. L. Guzmán, T. Hägglund. Tuning rules for feedforward control from measurable disturbances combined with PID control: A review. International Journal of Control, 2021.



6. End of design.

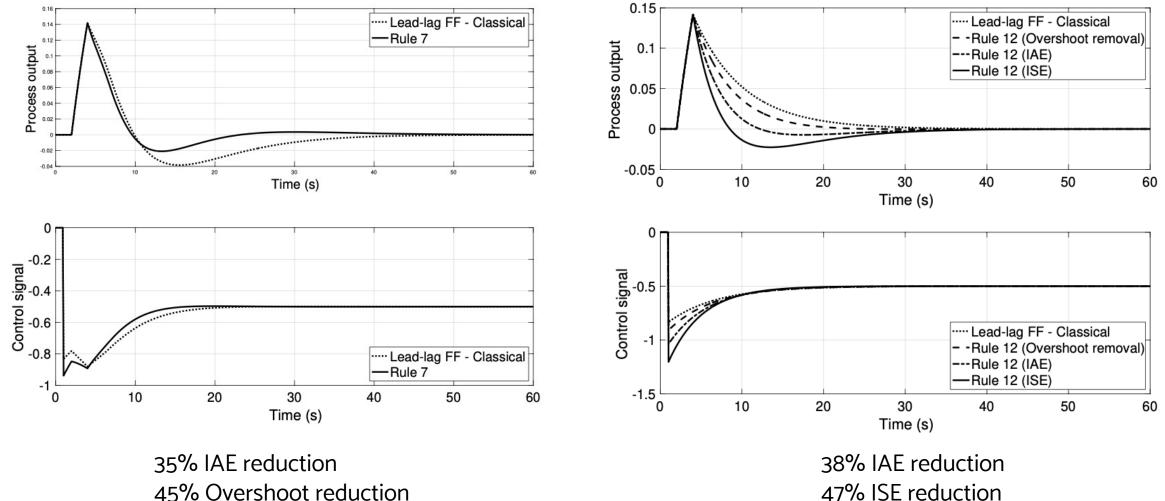








Non-interactive scheme



47% ISE reduction



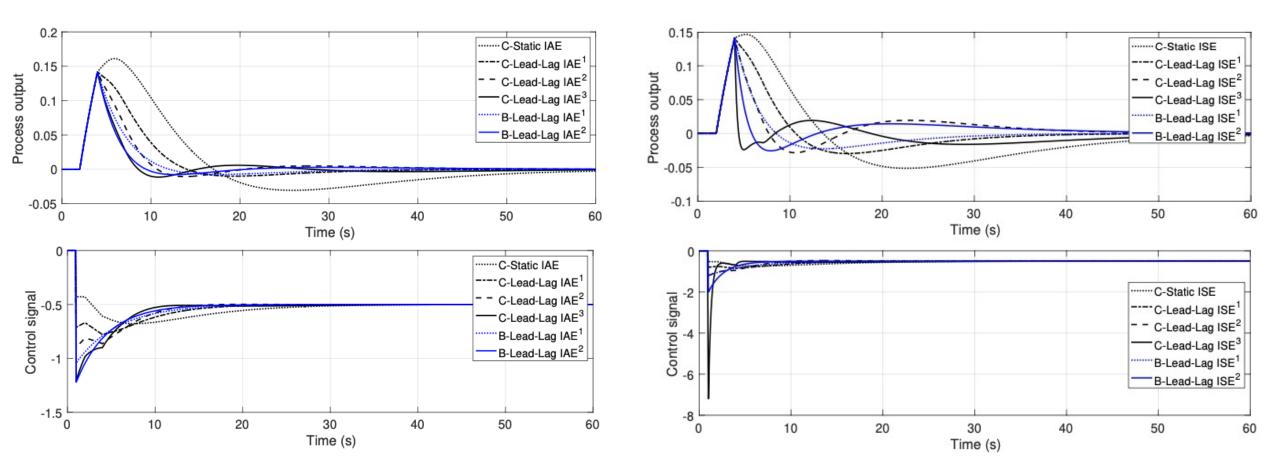








#### **Obtaining optimal tuning values**



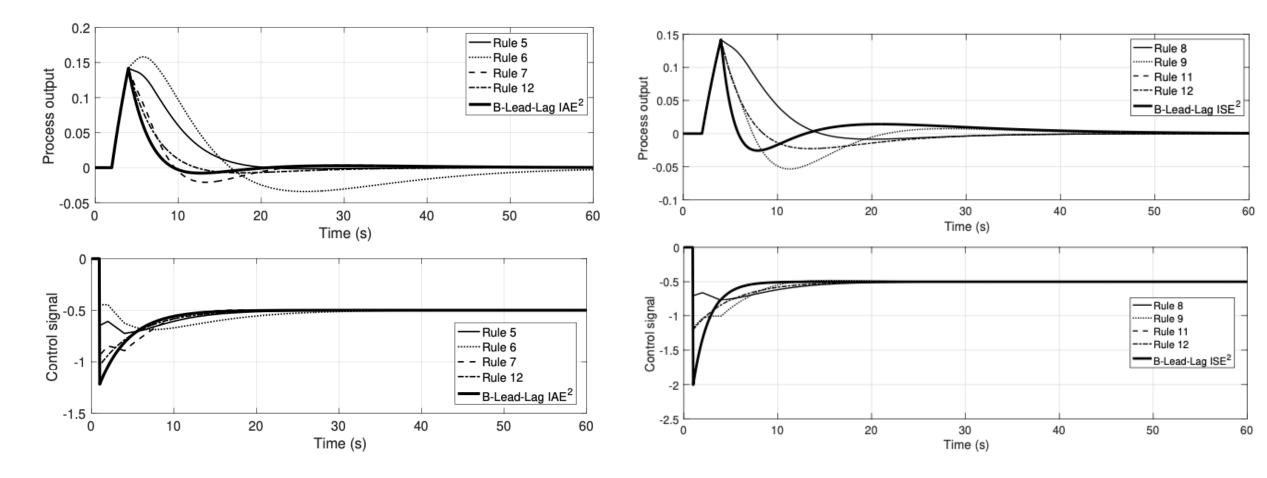


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#### Comparing the rules with the optimal rule





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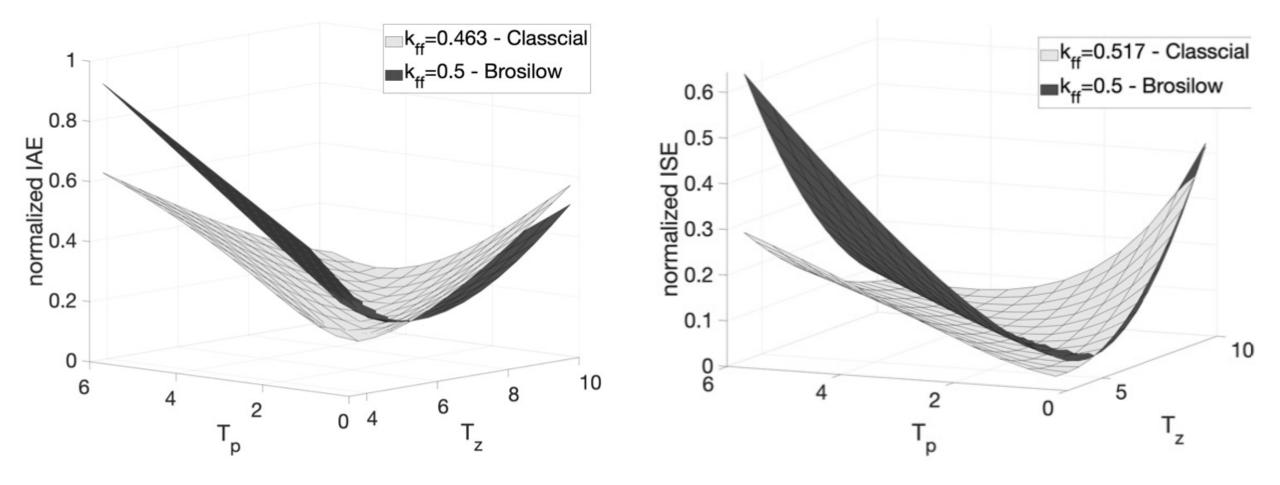


Rules	IAE <sub>norm</sub>	ISE <sub>norm</sub>	overshoot	peak	$k_{ff}$	$T_z$	$T_p$
FB	1	1	0	9.57	_	—	_
Static	0.477	0.182	9.1	44.69	0.5	_	_
Lead-Lag	0.257	0.082	7.67	76.28	0.5	10	6
Rule 1	0.284	0.139	0	36.47	0.358	10	6
Rule 2	0.514	0.324	2.5	23.54	0.306	_	_
Rule 3	0.236	0.116	0.22	44.15	0.386	10	6
Rule 4	0.18	0.084	0.56	57.97	0.414	10	5.5
Rule 5	0.232	0.113	0.3	45.07	0.389	10	6
Rule 6	0.461	0.199	6.8	37.6	0.446	—	_
Rule 7	0.166	0.059	4.18	87.79	0.453	10	4.824
Rule 8	0.212	0.094	1.7	54.29	0.422	10	6
Rule 9	0.207	0.061	10.66	136.17	0.491	10	4.158
Rule $10 (OS)$	0.18	0.084	0.56	57.97	0.414	10	5.5
Rule 10 (IAE)	0.166	0.059	4.18	87.79	0.453	10	4.824
Rule 10 (ISE)	0.207	0.061	10.66	136.17	0.491	10	4.158
Static	0.682	0.363	0	0	0.5	—	_
Lead-Lag	0.229	0.089	0	66.67	0.5	10	6
Rule 11	0.151	0.033	5.13	301.57	0.5	6.789	1.691
Rule $12 (OS)$	0.174	0.07	0.06	81.82	0.5	10	5.5
Rule 12 (IAE)	0.143	0.053	1.46	107.32	0.5	10	4.824
Rule 12 (ISE)	0.16	0.047	4.53	140.51	0.5	10	4.158









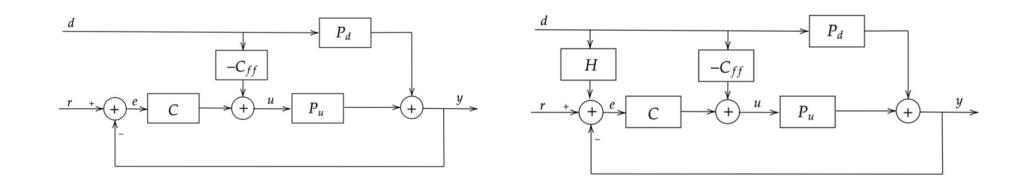












$$I_{FF/FB} = 1 - \frac{IAE_{FF}}{IAE_{FB}},$$

where  $IAE_{FB}$  is the integrated absolute value of the control error obtained when only feedback is used, and  $IAE_{FF}$  is the corresponding IAE value obtained when feedforward is added to the loop.

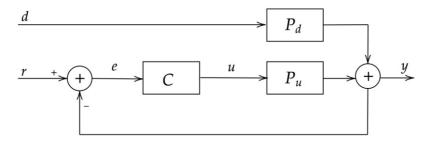
As long as the feedforward improves control, i.e.  $IAE_{FF} < IAE_{FB}$ , the index is in the region  $0 < I_{FF/FB} < 1$ .





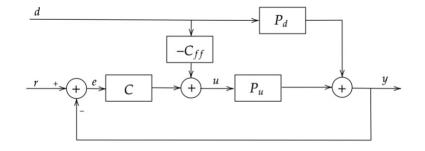
Performance indexes

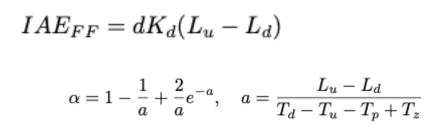


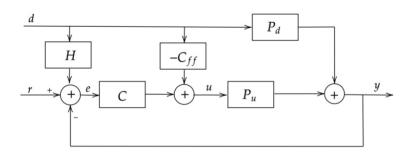


$$IAE_{FB} = K_d(\lambda + L_u)d$$

$$IAE_{FF} = K_d \left( L_1 - \tau \left( 1 - 2e^{-L_1/\tau} \right) \right) d$$
  
$$\tau = T_d - T_p \text{ and } L_1 = \max(0, L_u - L_d)$$













Rules	$IAE^{r}$	$IAE^e$	$\mathbf{I}^r_{FF/FB}$	$\mathbf{I}^{e}_{FF/FB}$
FB	4.371	4.372	Ó	Ó
Static	2.116	1.549	0.516	0.646
Lead-lag	1.125	1.096	0.743	0.749
Rule 5	1.014	0.971	0.768	0.778
Rule 6	2.043	1.46	0.533	0.666
 Rule 7	0.727	0.627	0.834	0.857
Lead-lag	1.0000	1.000	0.771	0.771
Rule 12	0.627	0.627	0.857	0.857



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$$\frac{IAE_{\text{classical}}}{IAE_{\text{noninteracting}}} = \frac{2(L_u + \lambda)f(\lambda/T_d)}{T_d} \qquad \qquad f(\lambda/T_d) = \begin{cases} \left(\frac{\lambda}{T_d}\right)^{-\frac{\lambda}{\lambda - T_d}} & \lambda \neq T_d \\ e^{-1} & \lambda = T_d \end{cases}$$

Therefore, the classical scheme gives a smaller IAE value when

 $T_d > 2(L_u + \lambda)f(\lambda/T_d)$ 

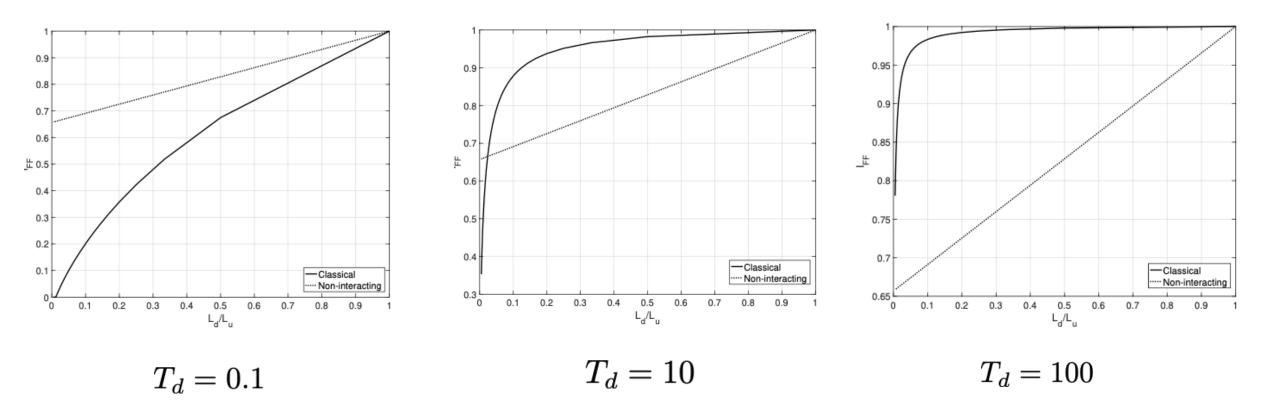
Since  $0 < f(\lambda/\tau) \le 1$ , one can conclude that the classical scheme gives a better performance when  $T_d$  is large compared to process dead time  $L_u$  or the desired closed-loop time constant  $\lambda$ , i.e. when the load disturbance is varying slowly.













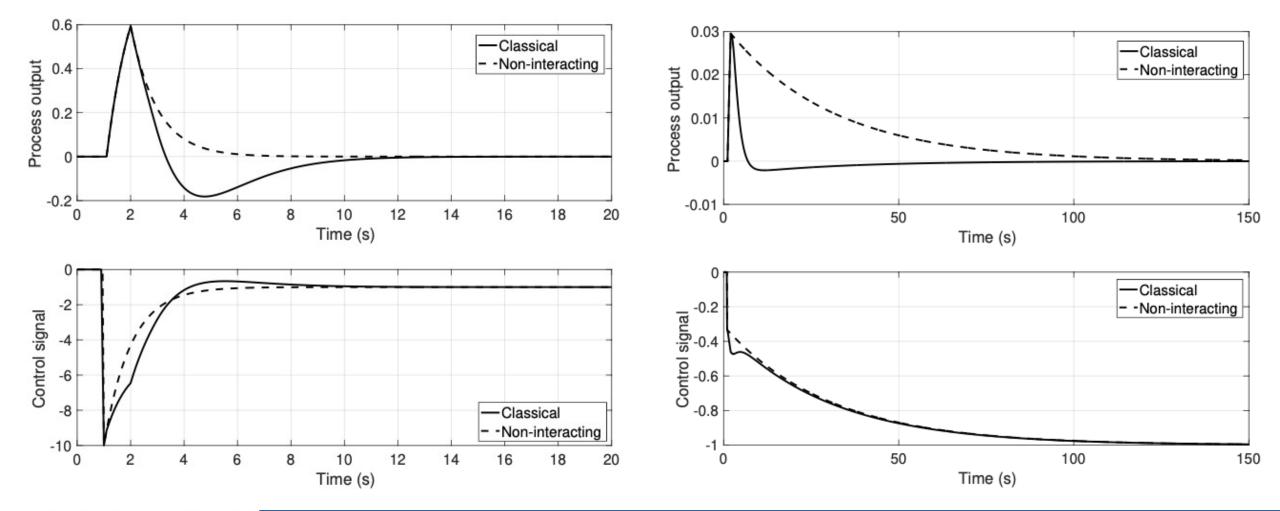
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$$T_d = 1 < 2(L_u + \lambda)f(\lambda/T_d) = 1.497$$

 $T_d = 30 > 2(L_u + \lambda)f(\lambda/T_d) = 4.832$ 





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## Conclusions



- The motivation for feedforward tuning rules was introduced.
- The two available feedforward control schemes were used.
- Simple tuning rules based on the process and feedback controllers' parameters were presented for both control schemes.
- The proposed rules were compared with optimal tuning parameters.
- The effect of feedforward compensator parameters was analyzed and combined with the selection of the feedforward control schemes.
- Performance indices for feedforward control were proposed.





## References



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## IFAC PID 2024



P202024

4th IFAC Conference on Advances in Proportional – Integral – Derivative Control (PID2014)

Almería, June 12-14 2024

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Important Dates: Oct 15, 2023 Subn

Oct 15, 2023Submission OpenDec 15, 2023Submission DeadlineMar 1, 2024Notification of AcceptanceMar 15, 2024Early Registration DeadlineMay 1, 2024Late Registration Deadline

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Thank you very much for your attention!