Some minimal representation-infinite algebras

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Abstract

A finite-dimensional K-algebra A (associative, with 1) is said to be minimal represention infinite, provided there are infinitely many isoclasses of indecomposable A-modules, and almost all are faithful. We are going to describe in detail two related classes of minimal representation-infinite algebras and their module categories, namely the "barbell algebras" and the "windwheel algebras". All these algebras are obtained from hereditary algebras of type A by what we call barification.

The barbell algebras are non-polynomial growth algebras and are new examples of Gorenstein algebras of Gorenstein dimension 1. The windwheel algebras are 1-domestic and may have an arbitrary finite number of non-regular AR-components.