A class of Noetherian finitely presented algebras

Abstract

The search for new concrete classes of finitely presented algebras (defined by monomial relations) that satisfy some arithmetical properties (such as being a maximal order) recently gained a lot of interest. These algebras can be considered as semigroup algebras K[S]. In general, it remain unsolved problems to characterize when an arbitrary semigroup algebra K[S] is Noetherian and when it is a prime Noetherian maximal order. The former question has been resolved when S is submonoid of polycyclic-by-finite groups. The second question has been completely solved when S is an abelian monoid (Chouinard) and when S is a polycyclic-by-finite groups (Brown).

In this lecture we report on recent results (joint with Goffa and Okninski) that give an answer to the question when K[S] is a prime Noetherian maximal order in case S is a submonoid of a polycyclic-by-finite group. In order to obtain a characterization, we first investigate height one prime ideals of K[S]. It turns out that actions of S on the height one primes are crucial. Several applications are given. We finish with some examples illustrating the results. Also some related results will be presented.