

# Interpolating sequences in weighted Bergman spaces

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Let  $W : \mathbb{D} \rightarrow [0, \infty)$  be a measurable function and  $0 < p < \infty$ .  $A^p(W)$  is the space of all analytic functions  $f$  in  $\mathbb{D}$  such that

$$\|f\|_{p,W}^p = \int_{\mathbb{D}} |f(z)|^p W(z) dA(z) < \infty.$$

A sequence  $(z_n) \subset \mathbb{D}$  is said to be an interpolating sequence for  $A^p(W)$  if for any  $(a_n) \in \ell^p$  there exists  $f \in A^p(W)$  such that

$$f(z_n)(1 - |z_n|^2)^{-2/p} \left( \inf_{w \in D(z_n, r)} W(w) \right)^{-1/p} = a_n, \quad n \in \mathbb{N} (0 < p \leq 1)$$

and

$$f(z_n)(1 - |z_n|^2)^{2/p} \left( \frac{1}{|D(z_n, r)|} \int_{D(z_n, r)} W^{-p'/p} \right)^{-1/p'} = a_n, \quad n \in \mathbb{N} (1 < p < \infty),$$

where  $D(z, r)$  denotes the hyperbolic disk.

Aleman and Vukotic proved [1]) that any uniformly separated sequence is interpolating for  $A^p(W)$  in the case of radial weights which are normal. We extend this result to non radial weights under certain  $A_1$ -condition for the averaging operator, extending the previously mentioned result.

Keywords. Interpolating sequences, weighted Bergman spaces,  $A_1$ -condition

## References

- [1] Aleman, A, Vukotic, D. *On Blaschke products with derivatives in Bergman spaces with normal weights*, J.Math. Anal. Appl., **361** (2010), 492–505.

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