



Analysis and validation of grid DEM generation based on Gaussian Markov Random Field

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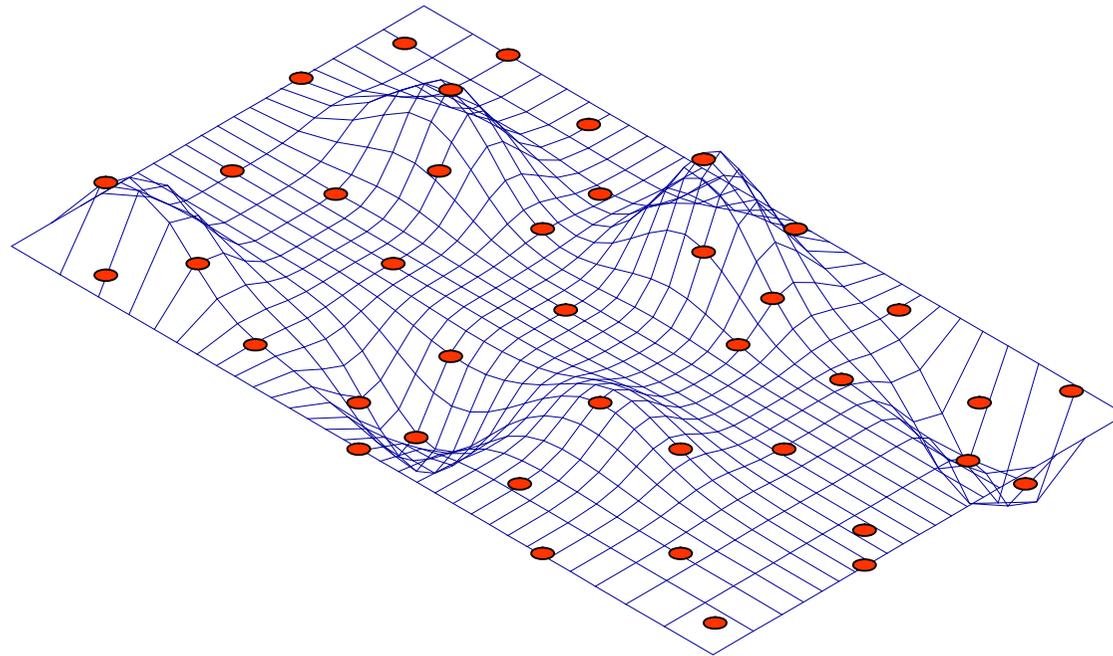


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Introduction

Goal:

Efficient generation of accurate Grid Digital Elevation Models from scattered elevation data including grid elevations uncertainty estimate



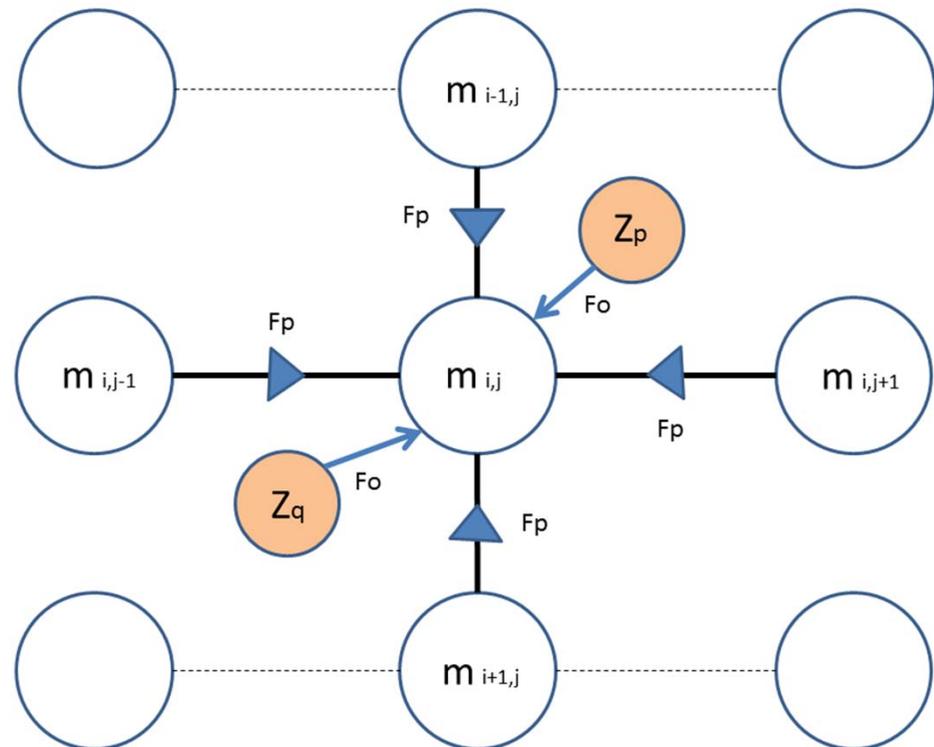
Introduction: Mathematical Framework

Gaussian Markov Random Field (GMRF) to estimate the maximum a posteriori (MAP) grid elevations and their vertical uncertainty

Graphical model for involved Factors:

Observation Factors (Fo)

Prior Factors (Fp)



Introduction: Mathematical Framework

The joint probability distribution to be maximised would be the following one:

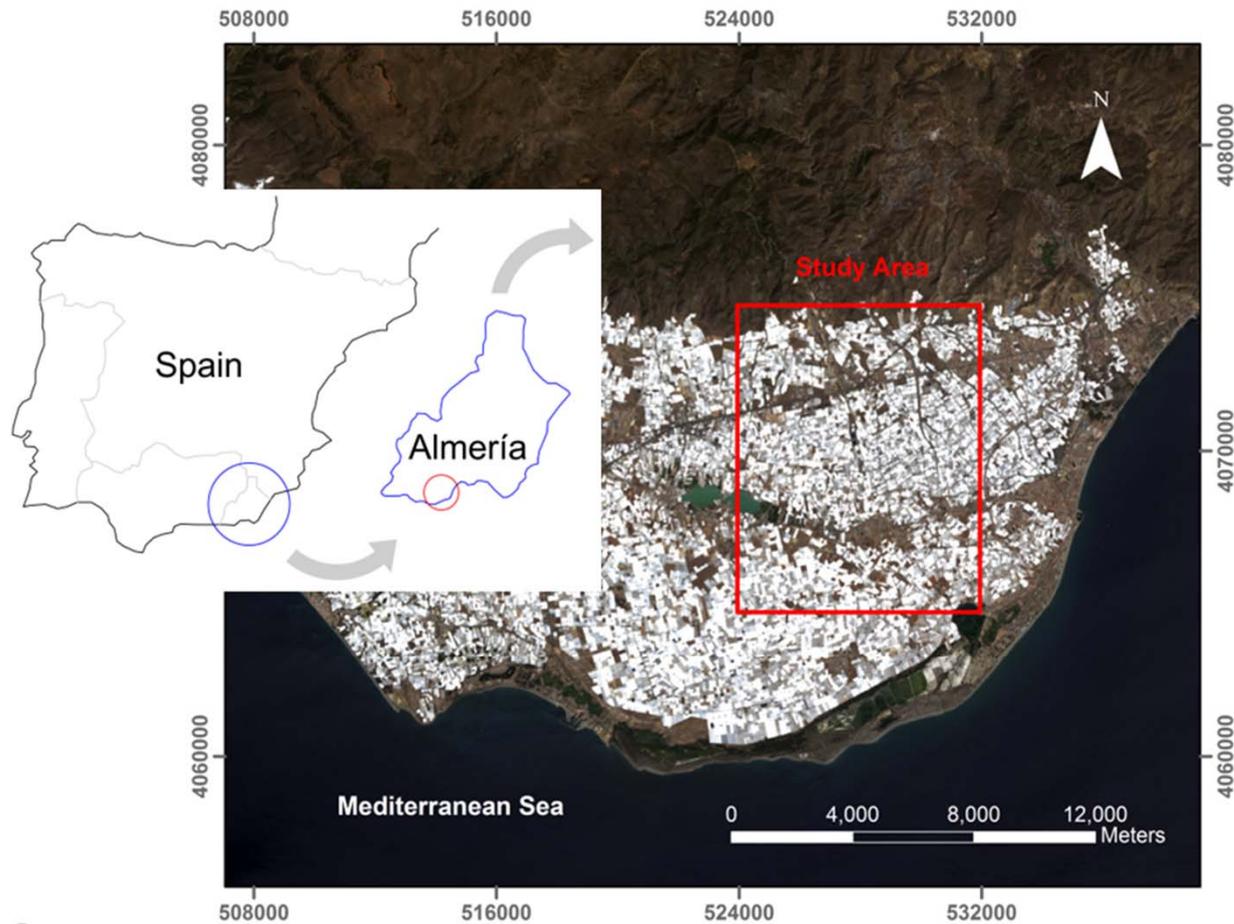
$$p(m, z) \propto e^{\left(- \sum_{C_o} E_o(n_{C_o}) - \sum_{C_p} E_p(n_{C_p}) \right)}$$

$$\left\{ \begin{array}{l} E_p = \sum_{C_p} E_p(n_{C_p}) = \sum_{k=1}^L \frac{(m_{ik} - m_{jk})^2}{\sigma_p^2 / (1 - P(d_{i,j}))^2} \\ E_o = \sum_{C_o} E_o(n_{C_o}) = \sum_{k=1}^M \frac{(m_{ik} - z_k)^2}{\sigma_s^2} \end{array} \right.$$

$$\sigma_s = \left(\frac{6}{\sqrt{n}} + 50 \cdot \tan \alpha \right) / 100 \quad \text{Karel \& Kraus (2006)}$$

Study Site and Dataset

Very dense greenhouse covered area located at Almería, southern Spain



Study Site and Dataset

Coloured LiDAR point cloud from PNOA (National Plan of Aerial Orthophotography of Spain).

Sensor: **Leica ALS60**; Flight Height: **2700 m**; Date: September 2015

Point density: **0.87 points/m²**; Single point returns

Reference System: ETRS89 UTM 30N; Orthometric elevations (EGM08-REDNAP)

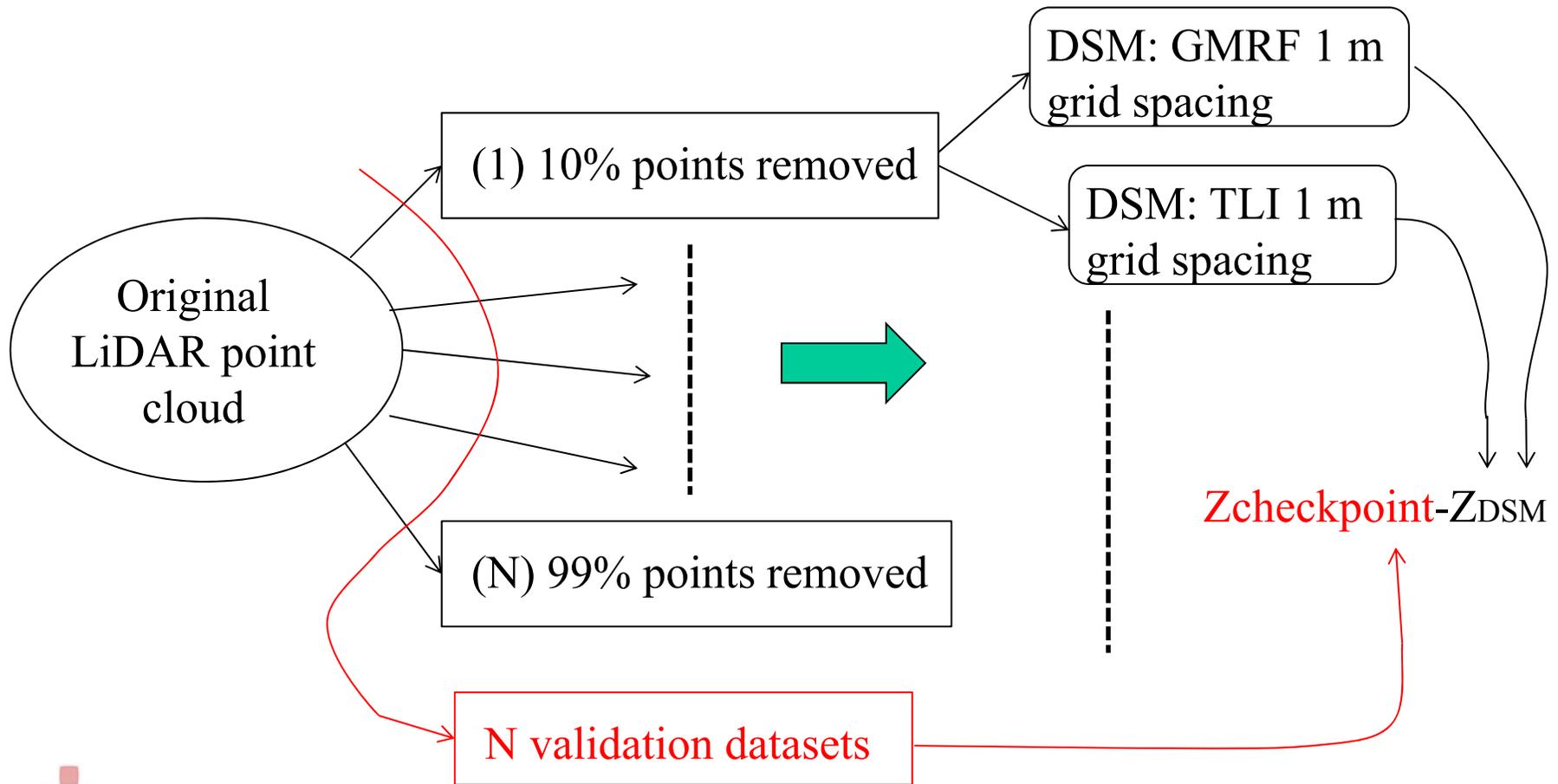
Vertical error (at open terrain GPS-RTK derived Check Points): **0.14 m**



450

Methods

DSM accuracy assessment



Results: Sensitivity analysis for σ_p

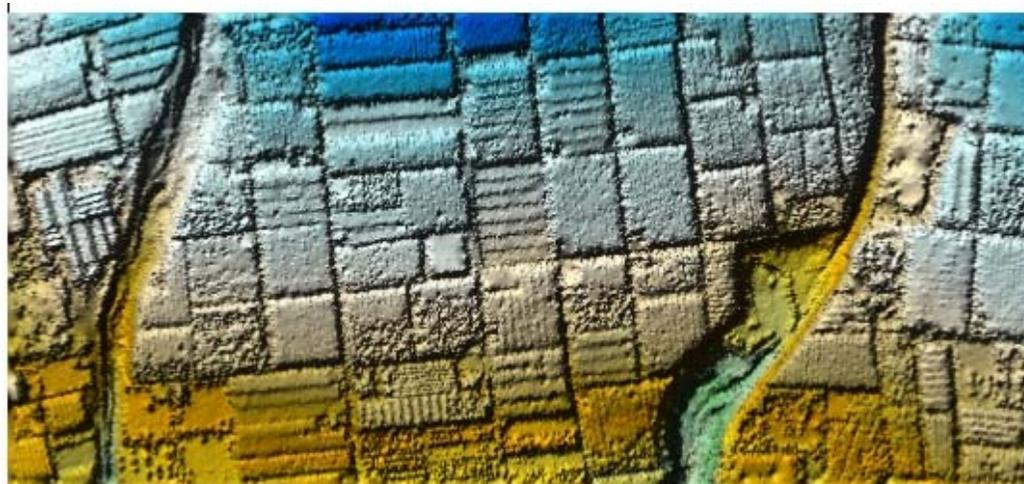
The lower the tolerance parameter, the higher the smoothing
GMRF derived DSM

Observed points: 10% of the original dataset ⁽¹⁾			Observed points: 1% of the original dataset ⁽²⁾		
σ_p (m)	rmse _z (m)	mean error (m)	σ_p (m)	rmse _z (m)	mean error (m)
0.2	0.803	0.008	0.2	1.274	0.011
0.6	0.765	0.013	0.6	1.186	0.002
1	0.765	0.002	1	1.148	0.011
1.4	0.761	0.007	1.4	1.146	0.029
1.8	0.758	0.008	1.8	1.141	-0.0018
2.2	0.760	0.003	2.2	1.143	0.010
2.6	0.761	0.002	2.6	1.158	-0.001
3	0.762	0.008	3	1.140	0.000
4	0.761	0.004	4	1.153	0.008
10	0.761	0.007	10	1.162	0.031

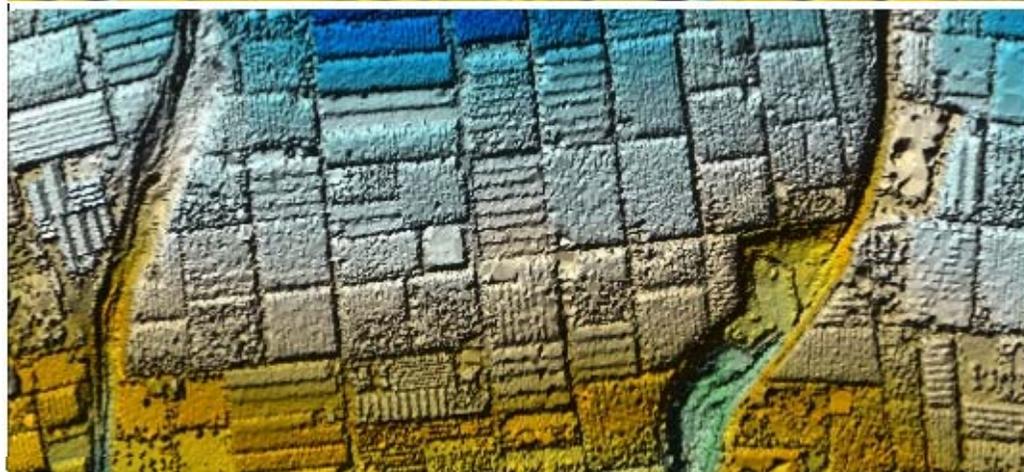
EGS (1) = 10.74 m; EGS (2) = 33.97 m

Results: GMRF vs TLI

Qualitative comparison (case 10% observed points; EGS = 10.74 m)



1 m GMRF DSM

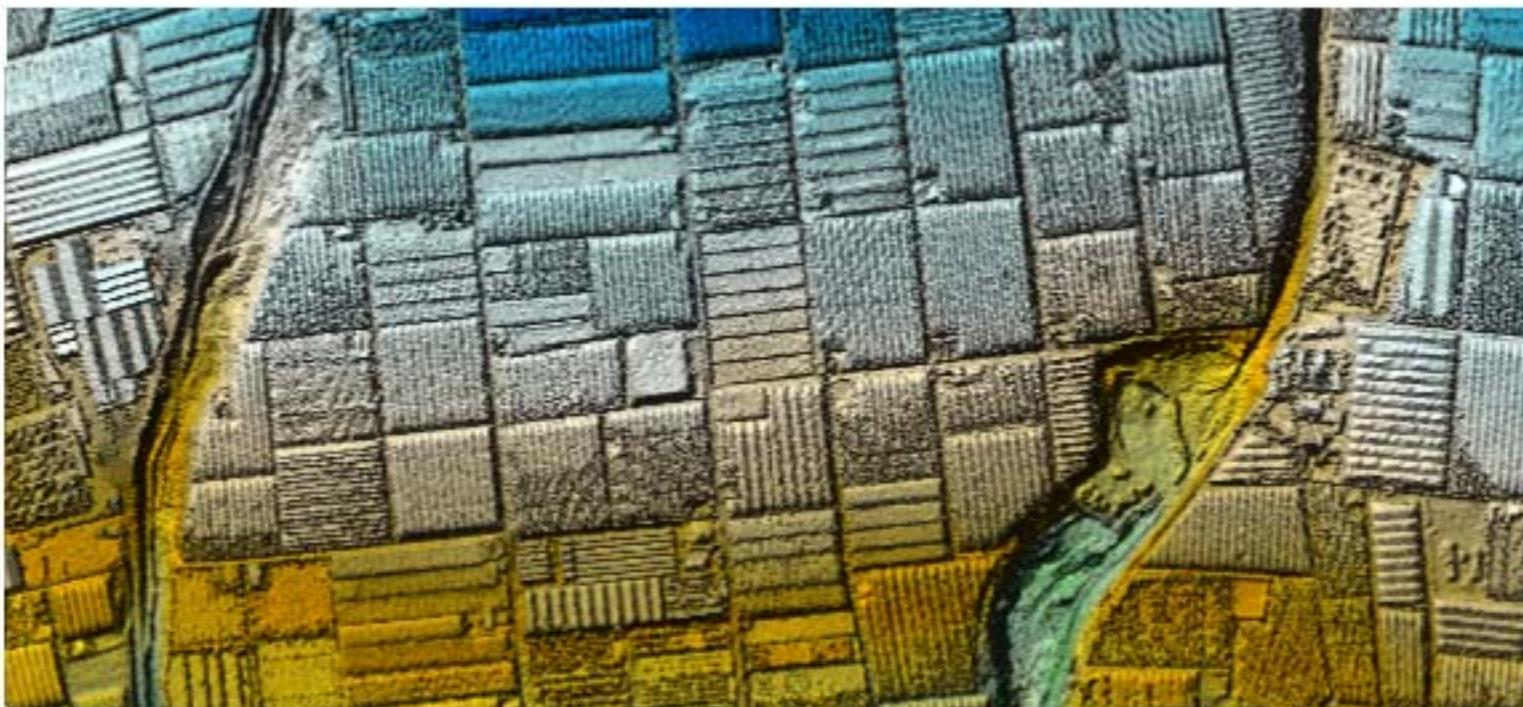


1 m TLI DSM

Results: GMRF vs TLI

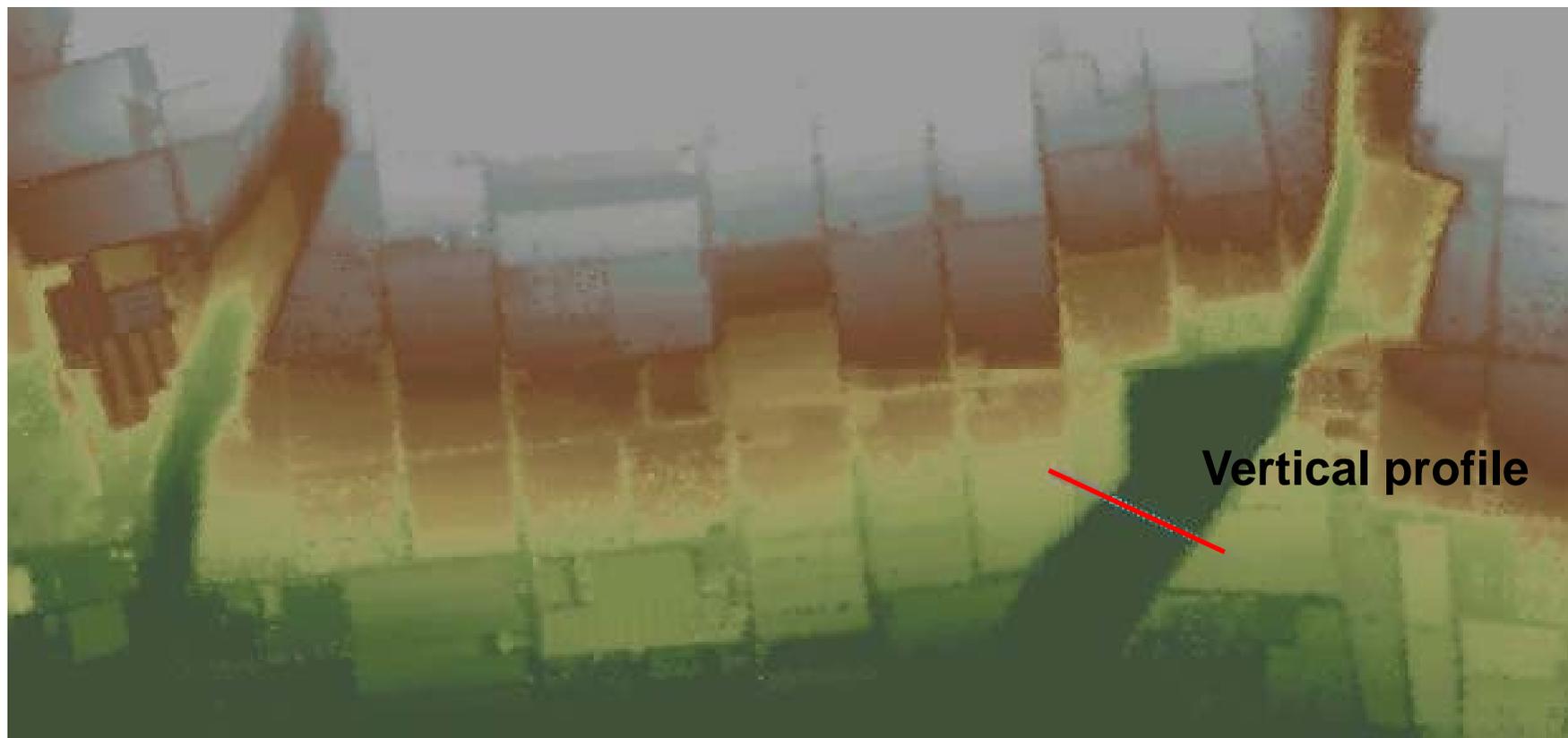
Qualitative comparison (case 90% observed points; EGS = 1.13 m)

1 m GMRF DSM



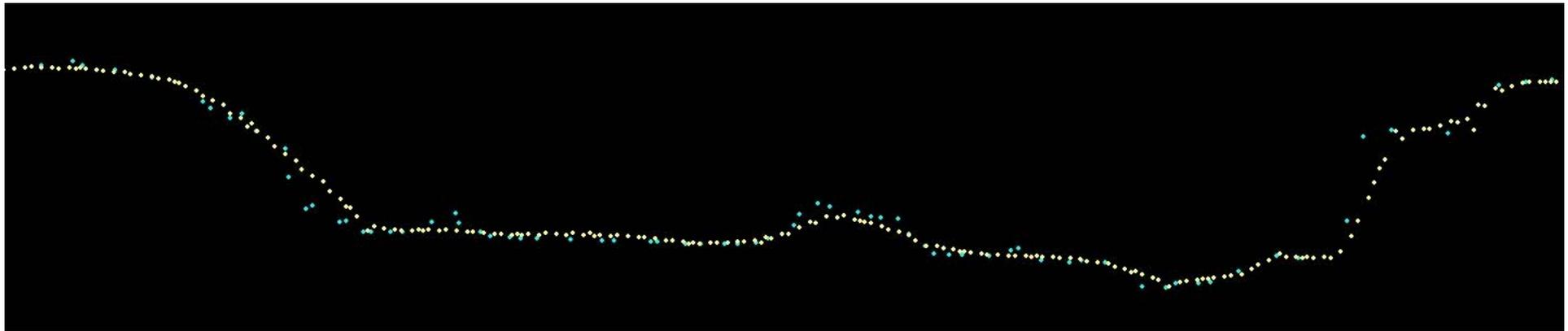
Results: GMRF vs TLI

Qualitative results



Results: GMRF vs TLI

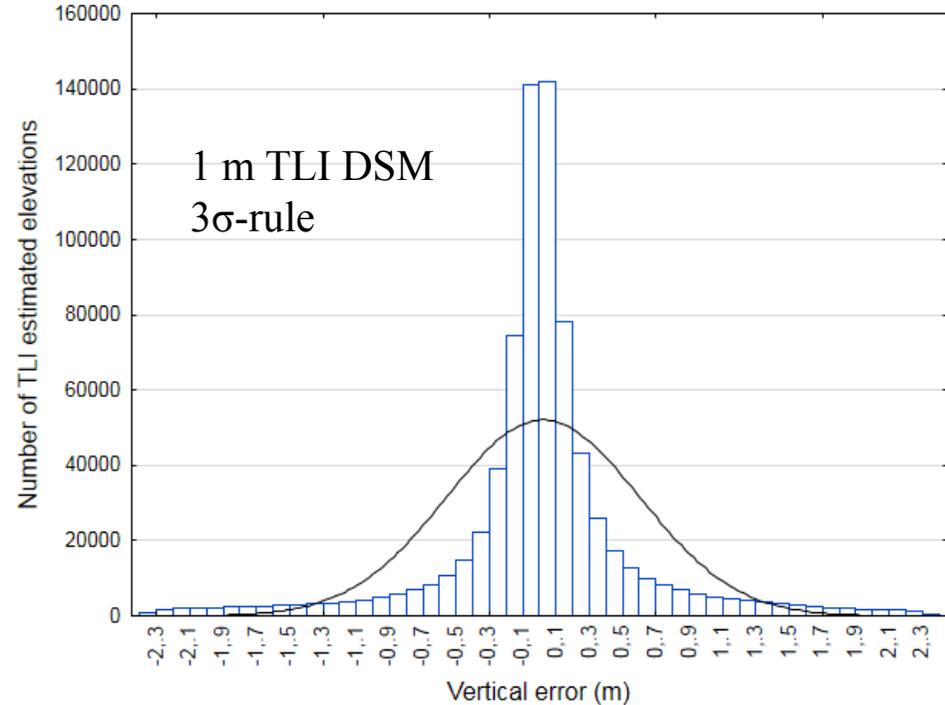
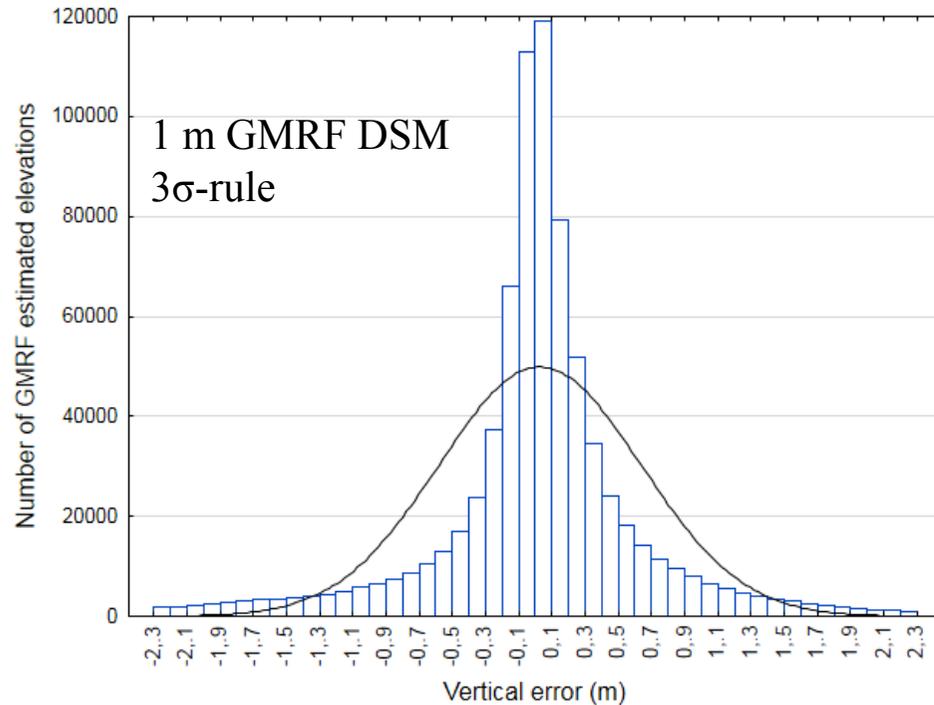
Qualitative results (10% observed points; EGS = 10.74 m)



- 1 m GMRF DSM
- LiDAR points

Results: GMRF vs TLI

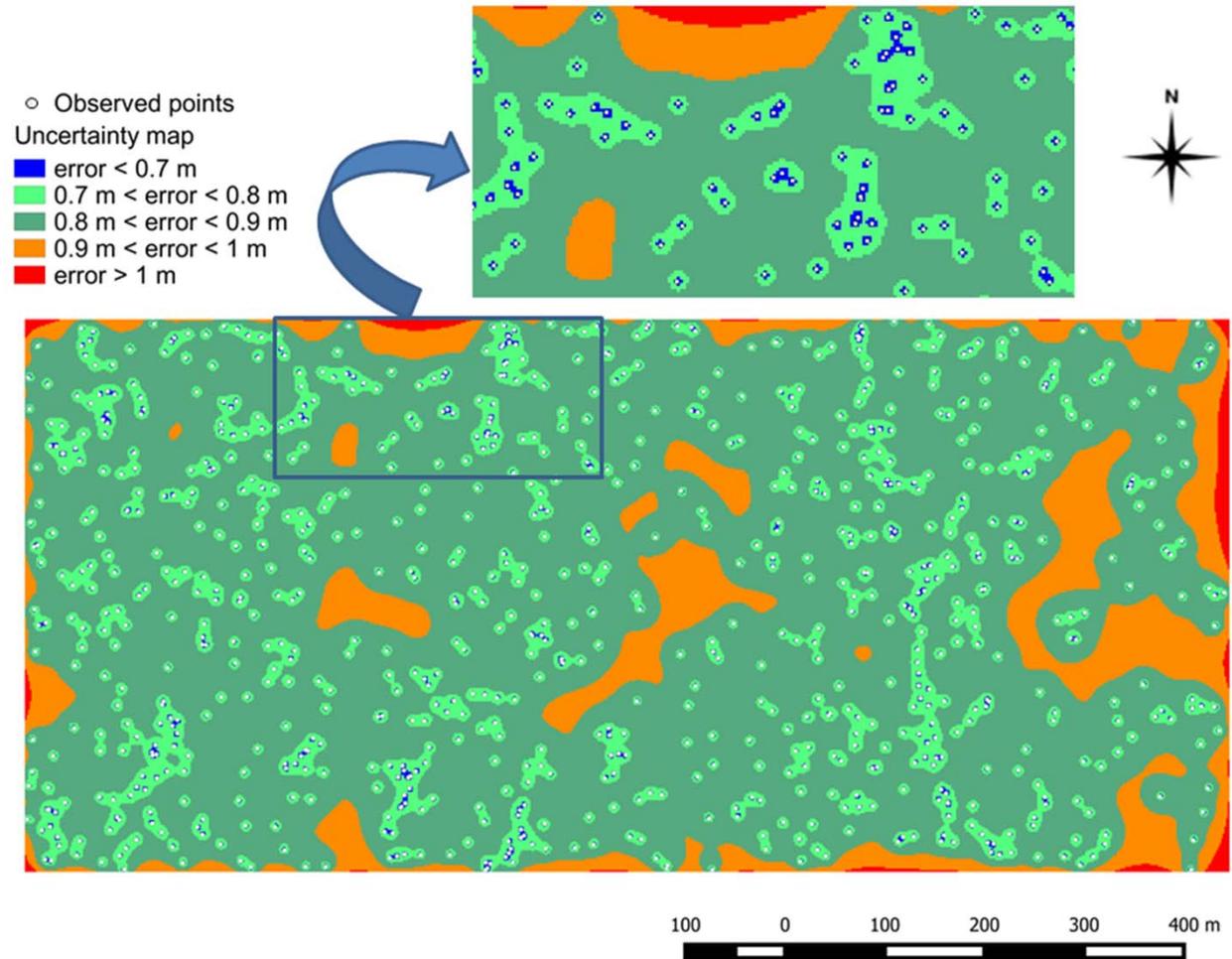
Quantitative results (10% observed points; EGS = 10.74 m)



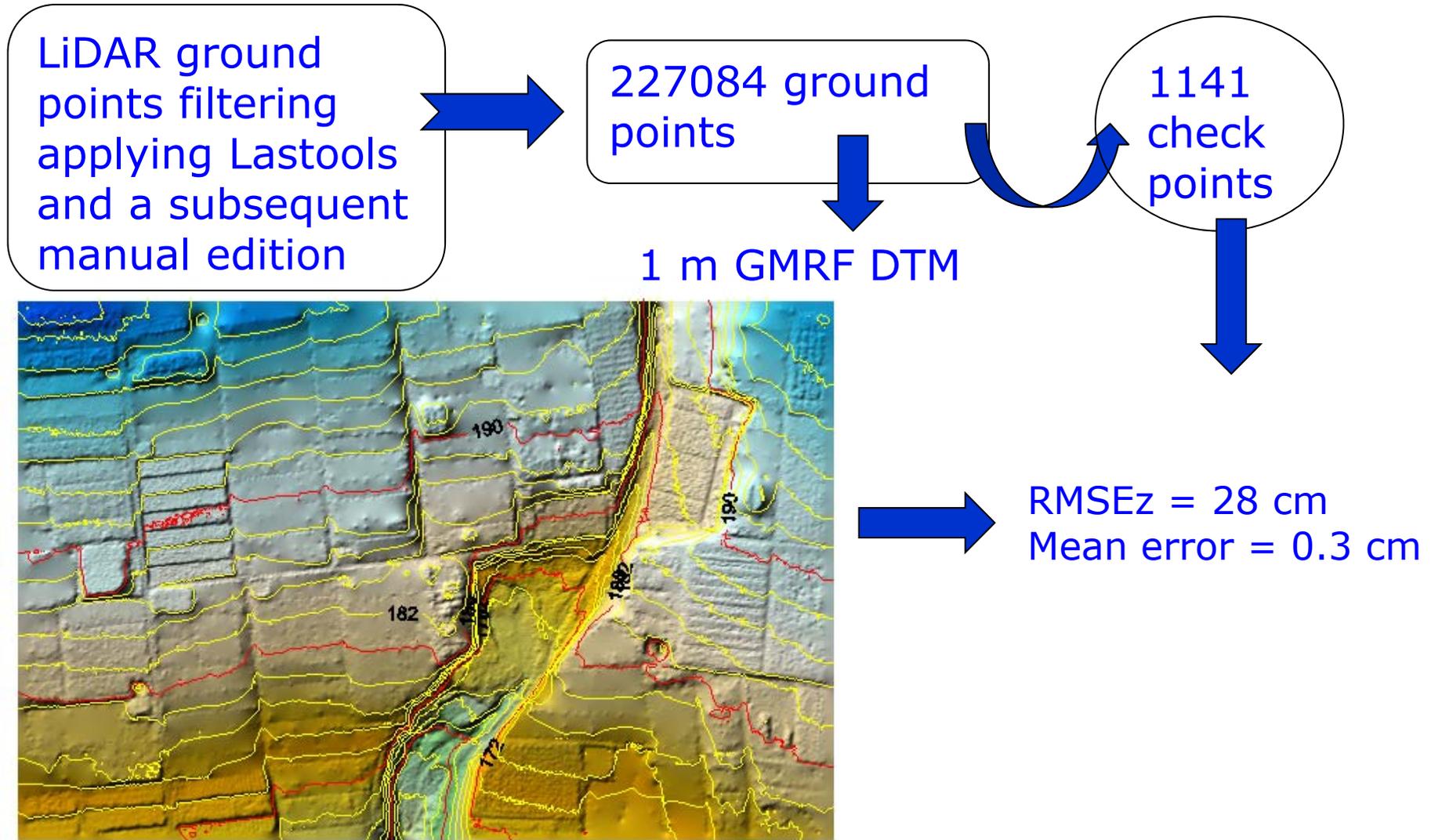
Leptokurtic and unbiased residual distributions

Results: DSM vertical uncertainty

2 m GMRF DSM



Results: Real-world application



Conclusions

The results provided by the proposed GMRF interpolation method may be deemed as very promising, producing visually pleasing and accurate digital elevation models.

GMRF yielded similar qualitative and quantitative results as compared to TLI method. Both methods do not require to specify the local support or kernel.

As a bonus, the mathematical framework implemented through GMRF algorithm makes possible to easily retrieve the maximum a posteriori estimation of every interpolated elevation point (mapping vertical uncertainty) and also include break lines, at least theoretically, to obtain high quality DTMs.



**Thank you very much for
your kind attention**



Open code available at:
<https://github.com/3DLAB-UAL/dem-gmrf>