## Lattice theory and module theory

Pascual JARA (University of Granada, Spain) pjara@ugr.es

Our aim in this talk is twofold. First we study decomposition of lattices and the consequences in the module theory. It is well known that if a ring R has a ring decomposition, the lattice of right ideals is a direct product of two module lattices. We study what happens whenever the lattice of a right R-module has such a decomposition, and apply it in different contexts. For the second approach let us consider a poset P, the preadditive category  $\mathcal{P}$ , and the well known functor category Mod- $\mathcal{P}$ . Working in Mod- $\mathcal{P}$  we build a hereditary torsion theory, and a class of modules that parameterizes the category of fuzzy modules over a given ring, and provide a well founded algebraic approach.